

Factors and Multiples

In this unit, students learn about factors and multiples and apply their understanding of the area of rectangles. Students determine if a number between 1 and 100 is prime or composite.

Section A: Understand Factors and Multiples

In this section, students learn about the meaning of factors and multiples by relating them to the concept of area. They use square tiles to build rectangles with given length and width. Then, they find the area of the rectangles.

7

We can say that 7 and 2 are a factor pair of 14, and that $7 \times 2 = 14$.

We can also say that 14 is a multiple of 7 and a multiple of 2.

Students discover that some numbers have many factor pairs and others have only one possible factor pair. They decide if a number is prime or composite based on how many rectangles can be made with that number as the area.

For example, this rectangle has an area of 14 square units with side lengths of 7 and 2.

Section B: Find Factor Pairs and Multiples

In this section, students apply what they learned about factors and multiples to play games and solve problems in different contexts. Through the tasks, students look for patterns with factors and multiples. They find all of the factor pairs of a whole number between 1–100. They also decide if a whole number within 100 is a multiple of a given one-digit number.

Try it at home!

Complete the statements for each number. Explain your reasoning.

number	factor	multiple
5	is a factor ofbecause	is a multiple of because
18	is a factor ofbecause	is a multiple ofbecause



- How did you know this was a factor of that number?
- How did you know this was a multiple of that number?
- How are factors related to multiples?
- Is the number prime or composite? How do you know?



Fraction Equivalence and Comparison

In this unit, students deepen their knowledge of fractions. They explore the size of fractions, write equivalent fractions, and compare and order fractions with the denominators 2, 3, 4, 5, 6, 8, 10, 12, and 100.

Section A: Size and Location of Fractions

In this section, students revisit the meaning of fractions. They use fraction strips, tape diagrams, and number lines to represent fractions. Students compare fractions with the same numerators or the same denominators, and recall that equivalent fractions have the same size.

Students consider the size of fractions whose denominators are related, such as $\frac{1}{5}$ and $\frac{1}{10}$, or $\frac{1}{6}$ and $\frac{1}{12}$. They also compare fractions to benchmarks such as $\frac{1}{2}$ and 1. (For instance, they see that $\frac{3}{10}$ is less than $\frac{1}{2}$ and $\frac{3}{5}$ is more than $\frac{1}{2}$.)

Section B: Equivalent Fractions



For example, they can explain that the fraction $\frac{2}{3}$ is equivalent to $\frac{8}{12}$ because the numerator and the denominator of $\frac{2}{3}$ are each multiplied by the same number, 4, to get $\frac{8}{12}$. Students use such observations to identify and write equivalent fractions.

Section C: Fraction Comparison

In this section, students compare fractions with different numerators and denominators using various strategies. For example, they may think about how far each fraction is from 0 on a number line, how each fraction compares to $\frac{1}{2}$ or 1, or think of the fractions in terms of the same denominator.



Students record the results of comparisons with symbols >, =, or <. They then solve problems that involve comparing fractional measurements, such as lengths in fractions of an inch.

Try it at home!

Near the end of the unit, ask your student to compare $\frac{3}{5}$ and $\frac{3}{7}$.

- How are the two fractions alike? How are they different?
- What strategy did you use to compare?
- Is there a different strategy that you could use to compare?



Extending Operations to Fractions

In this unit, students think about how fractions can be composed (put together) and decomposed (taken apart). They also learn about fraction operations: multiplying fractions and whole numbers, adding and subtracting fractions with the same denominator, and adding tenths and hundredths.

Section A: Equal Groups of Fractions

Previously, students thought about multiplication as equal groups of whole numbers of objects, such as 5 bags with 2 oranges in each bag. In this section, they think about equal groups of fractional pieces, such as 5 plates with $\frac{1}{2}$ orange on each plate. They see that the amount can be represented by $5 \times \frac{1}{2}$, which is $\frac{5}{2}$.



Students then make sense of diagrams and equations that represent the multiplication of a whole number and a fraction, such as $4 \times \frac{2}{3} = \frac{8}{3}$.

They learn that the numerator in the resulting fraction is the product of the whole number (the 4) and the numerator of the fractional factor (the 2 in $\frac{2}{3}$), and the denominator is the same as in the fractional factor (the 3 in $\frac{2}{3}$).

Diagrams can help students see that some fractions can be represented by more than one multiplication expression. For example, the diagram shows that the following expressions all have the value of $\frac{8}{3}$.



Section B: Addition and Subtraction of Fractions

In this section, students learn to add and subtract fractions by decomposing them into sums of smaller fractions, writing equivalent fractions, and using number lines.



Students first think about a fraction as a sum of other smaller fractions. They represent different ways to decompose a fraction by drawing "jumps" on number lines and writing different equations. Later, they use number lines to represent subtraction of fractions.



Working with number lines helps students see that a fraction greater than 1 can be decomposed into a whole number and a fraction, and then written as a mixed number. For example, to find the value of $3 - \frac{2}{5}$, it helps to first decompose the 3 into $2 + \frac{5}{5}$, and then subtract $\frac{2}{5}$ from the $\frac{5}{5}$ to get $2\frac{3}{5}$.

Section C: Adding Tenths and Hundredths

In this section, students learn to add tenths and hundredths. Previously, students learned that $\frac{1}{10} = \frac{10}{100}$. They use this reasoning to find equivalent fractions that can help them add tenths and hundredths.

Try it at home!

Near the end of the unit, ask your student to solve the following problems:

What equation is represented by the jump on the number line?



Find the value of $\frac{8}{10} + \frac{29}{100}$.

- How did you know those fractions were needed for the equation?
- How did you find your answer?
- How could you solve your problem in a different way?

From Hundredths to Hundred-thousands

In this unit, students learn to express small and large numbers, from hundredths to hundred-thousands. They learn to write tenths and hundredths using decimal notation and to work with whole numbers within 1 million.

Section A: Decimals with Tenths and Hundredths

In this section, students relate the fraction $\frac{1}{10}$ to the notation 0.1 and $\frac{1}{100}$ to 0.01. They learn to read 0.1 as "one tenth" and 0.01 as "one hundredth."

To connect the fraction notation, decimal notation, and word name of a fraction, students reason with square diagrams that each represent 1 and are partitioned into hundredths.

The gridded square helps students see that $\frac{1}{10}$ (or 0.1) and $\frac{10}{100}$ (or 0.10) represent the same amount. It also allows students to recognize other tenths and hundredths that are equivalent.

For instance, the shaded parts of this diagram represent both 40 hundredths ($\frac{40}{100}$) and 4 tenths ($\frac{4}{10}$), so 0.4 = 0.40.

Later in the section, students locate decimals on number lines. They compare decimals based on size and write comparison statements using the symbols <, >, and =.

Section B: Place-value Relationships through 1,000,000

In this section, students make sense of whole numbers up to the hundred-thousands place. They use base-ten blocks and diagrams to represent large numbers.

Students come to understand the value of the digit in each position in a multi-digit number. They see that a digit in one place has a value that is ten times the value of the same digit in a place to its right.

For example, the 3 in 347,000 has a value ten times that of the 3 in 34,700, because $300,000 = 10 \times 30,000$.



Section C: Compare, Order, and Round

In this section, they compare and round numbers within 1,000,000. To compare numbers, students think about the value of the digits and locate the numbers on a number line.

To round a number, they think about multiples of 10, 100, 1,000, 10,000, and 100,000 that are the closest to the number. For example, 215,300 rounded to the nearest hundred-thousand is 200,000.& Students then solve problems involving large numbers in various situations.



Section D: Add and Subtract

In this section, students learn to use the standard algorithm for addition and subtraction. As in earlier grades, they think about composing (putting together) or decomposing (or breaking apart) base-ten units to add and subtract.

To find the value of 17,375 + 14,024, for example, students may first write each number in expanded form and then add the values in each place (ten-thousands, thousands, hundreds, tens, ones). Later, they connect this way of adding to the standard algorithm for addition.

	10,000	+	7,000	+ 300 +	70	+	5			1	7 5
+	10,000	+	4,000	+ 0+	20	+	4		+	1 7, 3	24
	20,000	+	11,000	+ 300 +	90	+	9	= 31,399		3 1, 3	99

Try it at home!

Near the end of the unit, ask your student about the numbers 769,038 and 170,932:

- What is the value of the 7 in each number? Write a multiplication or division equation to show the relationship between these two values.
- Round each number to the nearest multiple of 1,000 and multiple of 100,000.
- Find the sum and difference of the two numbers.

- How did you find your answer?
- How could you solve your problem in a different way?



Multiplicative Comparison and Measurement

In this unit, students make sense of multiplication as a way to compare quantities. They use this understanding to convert units of measurement and to solve problems about measurement.

Section A: Multiplicative Comparison

In this section, students learn to compare quantities in terms of multiplication. In a multiplicative comparison, the underlying question is "how many times as many?" (In contrast, in an additive comparison, the question is "how many more (or less)?")

Students begin with comparisons that involve small factors and familiar situations, using familiar multiplicative comparison language (such as "twice," or "twice as many").

For example, students learn that they can compare the number of cubes in the image by saying, "Han has 2 times (or twice) as many cubes as Andre."



As larger factors and more abstract situations are introduced, students interpret and use abstract tape diagrams where each section of the diagram is labeled to represent any quantity.

In this example, while we do not know how many cubes Andre has, we know that Jada has 3 times as many cubes as Andre.



Section B: Measurement Conversion

In this section, students expand their knowledge of units of measurement from earlier grades. Previously, they learned that there are 100 centimeters in 1 meter. Here, they relate centimeters and meters in terms of multiplication—1 meter is 100 times as long as 1 centimeter—and use this reasoning to convert any number of meters to centimeters.

Students also relate other units of measurement in terms of multiplication: meters and kilometers, grams and kilograms, milliliters and liters, ounces and pounds, and seconds, minutes, and hours. They then solve problems that involve converting a larger unit to a smaller unit.

Section C: Let's Put it to Work

In this section, students use multiplicative comparison and measurement conversion to solve multi-step problems. They convert units of length, weight, and capacity in the metric system and customary system (working with length units such as yards, feet, and inches, and capacity units such as gallons, quarts, and cups).

As they solve problems, students develop their sense of the relative size of these units.

For a potluck party, Priya and three other relatives are bringing mango lassi. Who prepared the most mango lassi? How many cups of lassi did all the guests bring?



guest	amount of mango lassi
Priya	10 cups
Uncle	3 quarts
Cousin	8 cups
Grandma	2 gallons

Students also solve problems in geometric contexts. They analyze the relationship between the side lengths and perimeter of quadrilaterals and perform unit conversion along the way.

Try it at home!

Near the end of the unit, ask your student to solve the following problem:

A paint store sold 79 gallons of paint the first week it opened. The following week, the paint store sold 4 times as many gallons of paint. How many gallons of paint did the paint store sell in the second week?

- Can you draw a diagram to show the multiplicative comparison?
- Can you write an equation that goes along with the story problem?
- How would you convert the amount of gallons to quarts? To cups?



Multiplying and Dividing Multi-digit Numbers

In this unit, students deepen their understanding of multiplication and division and expand their ability to perform these operations on multi-digit numbers.

Section A: Features of Patterns

In this section, students analyze patterns. They use ideas related to multiplication (such as factors, multiples, double, and triple) to describe and extend the patterns.

If the pattern continues, could 50 represent the side length or the area of one of the rectangles? If so, which step? If not, why not?



Section B: Multi-Digit Multiplication

In this section, students multiply one-digit numbers and numbers up to four digits, and pairs of two-digit numbers. They learn to use increasingly more efficient methods to multiply.

Students begin by using visual representations—arrays, base-ten diagrams, and grids—to help them find products. They recall that rectangles can be used to represent multiplication, with the side lengths representing the factors and the area representing the product.

Students see that it helps to decompose (break apart) the factors by place value. For example, to multiply 31 and 15, we can think of the 31 as 30 + 1 and the 15 as 10 + 5. We can then label these values on a diagram, multiply the parts separately, and add the partial products.

	30	1		3	1	
ſ		1	×	1	5	
10	10 × 20 - 200	$10 \times 1 - 10$			5	5 imes 1
	10 × 30 = 300	10 × 1 – 10	1	5	0	5 imes 30
				1	0	10 imes 1
_	5 20 450		+ 3	0	0	10 imes 30
5	$5 \times 30 = 150$	5 × 1 = 5	4	6	5	

Later, students use an algorithm that lists partial products vertically. This work prepares them to make sense of the standard algorithm for multiplication, to be studied closely in grade 5.



Section C: Multi-Digit Division

In this section, students divide larger numbers (up to four digits), explore new division strategies, and interpret division situations that involve remainders.

Students begin by solving various problems that involve division, including those about equal groups, factors and multiples, and area of rectangles. They recall that an expression such as $96 \div 8$ can be used to find how many groups of 8 in 96, or to find the size of one group if 96 are put into 8 groups.

Students see that just as they can multiply	two numbers by		
decomposing the factors and finding partia	1		
divide by decomposing the dividend (the nu	12		
and finding partial quotients. Thinking about	ut place value can	80	
help us as well.		5)465	
	400 7 00	- 400	5 imes 80
Students then learn to organize partial	$400 \div 5 = 80$	65	
quotients using equations and an	$60 \div 5 = 12$	- 60	5 imes 12
algorithm that records division vertically.	$5 \div 5 = 1$	5	
	$465 \div 5 = 93$	- 5	5 × 1

Section D: Let's Put It To Work: Problem Solving with Large Numbers

Students solve a variety of problems that involve all four operations on multi-digit numbers. The problems can be approached in many ways, allowing students to choose their methods and representations strategically. Many of them also involve multiple steps.

Try it at home!

Near the end of the unit, ask your student to solve the following problems:

- 16 × 48
- 324 ÷ 6

- Can you draw a diagram to help you solve the problem?
- Can you explain the steps of your algorithm?



Angles and Angle Measurement

In this unit, students learn new language for describing parts of geometric figures and practice identifying and drawing them. They also learn to talk about angles, measure their size, and draw angles of different measurements.

Section A: Points, Lines, Segments, Rays, and Angles

This section introduces students to some building blocks of geometric figures—points, rays, segments, angles, and lines. Students learn about parallel lines (lines that never intersect) and perpendicular lines (lines that meet or intersect at a right angle).



They also learn that an angle is a figure that is made up of two rays that share the same endpoint, called the vertex of the angle. Students practice identifying angles, noticing that angles are all around us and can have different sizes.

Section B: The Size of Angles

In this section, students compare and describe the size of angles. They begin by comparing angles visually, for example, by considering ways to describe the size of angles on a clock. The hands of a clock helps to show that an angle is formed when one ray rotates around a point shared with another ray.





Students then learn that angles can be measured, with degrees (°) as the unit of measurement, and that a ray that makes a full turn around a point makes a 360-degree angle.

Later in the section, students learn to use a protractor to measure angles and to draw angles.

Section C: Angle Analysis

In this section, students continue to draw and analyze angles and to reason about their measurement. They classify angles by their size and identify angles as right, acute, obtuse, and straight.

Students learn that angles can be added. To investigate this idea, they use paper cutouts, patty paper, and drawings. Students fold, cut, mark, and assemble pieces of paper to see how angles can be composed (put together) and decomposed (broken apart).



Later, students solve problems and find unknown angle measurements in different contexts.



Try it at home!

Near the end of the unit, ask your student to:

- Find an acute angle, obtuse angle, straight angle, right angle, and parallel and perpendicular lines around the house.
- Describe and measure some angles found around the house.

- How would you describe that figure? How do you know it is a _____?
- How does that angle compare to a right angle (or a straight angle)?



Properties of Two-dimensional Shapes

In this unit, students classify triangles and quadrilaterals based on the attributes of their sides and angles. They also learn about lines of symmetry in two-dimensional figures. Students then sue these attributes of figures to solve geometric problems, including those about perimeter and area.

Section A: Side Lengths, Angles, and Lines of Symmetry

In this section, students think about different attributes of two-dimensional shapes, such as:

- number of sides
- length of sides
- size of angles
- presence of parallel or perpendicular lines
- symmetry

They examine shapes, classify them by the attributes they share, and explain their classifications. For example, given examples of parallelograms and rhombuses, students think about what must be true about the sides and angles of each type of quadrilaterals.

Quadrilaterals N, U, and Z are parallelograms.

Quadrilaterals AA, EE, and JJ are rhombuses.





Students also learn about symmetry—whether a figure can be folded along a line into two equal halves that match up exactly. They draw lines of symmetry for given figures, and complete drawings of figures that are halved by a line of symmetry.





Section B: Reason About Properties to Solve Problems

In this section, students reason about measurements in shapes.

Students begin by finding the perimeter of shapes where the side lengths are all given. Then, they look at shapes where the side lengths are not all given but can be found because of the attributes of the shapes (for example, the opposite sides are the same length) or because the perimeter is known.

Figures P, Q, and R each have 1 line of symmetry. Figure Q has 4 lines of symmetry. All figures have a perimeter of 64 inches.



As they find perimeters and side lengths, students also practice performing operations on whole numbers and fractions.

Try it at home!

Near the end of the unit, ask your student to solve the following problems:

• What attributes do these figures all have in common? For each figure, how many lines of symmetry can you find?



• What shapes do you see around the home or in places we visit? How could we classify them into categories?

- Can you describe the attributes of these shapes?
- What does it mean to have a line of symmetry?



Putting It All Together

In this unit, students apply what they have learned throughout the year to strengthen major concepts and fluency goals of the grade.

Section A: Fraction Fun

In this section, students practice multiplying fractions and whole numbers, as well as adding and subtracting fractions with the same denominator. They also solve problems that involve comparing fractions and adding and subtracting tenths and hundredths.

> Here are the times of the runners for two teams. Which team won the relay race?

runner	Diego's team, time (seconds)	Jada's team, time (seconds)
1	$10\frac{25}{100}$	$11\frac{9}{10}$
2	$11\frac{40}{100}$	$9\frac{8}{10}$
3	$9\frac{7}{10}$	$9\frac{84}{100}$
4	$10\frac{5}{100}$	$10\frac{60}{100}$



Section B: Whole-number Operations

In this section, students deepen their understanding of place value and build their fluency in performing operations on multi-digit numbers.

Students begin by using the standard algorithm to add and subtract numbers within 1 million. They recall when to compose (or "carry") a new place-value unit (a ten, a hundred, a thousand, and so on) when adding, and when to decompose a unit (or "regroup") when subtracting.

Students learn to pay attention to potential errors, especially when subtracting a number with non-zero digits from a number with zeros, and to be more strategic in choosing a method.

Use both Priya and Han's methods to find	Priya						На	n					
the difference of 20,000 and 472.		2	0,	0	0	0					4	7	2
	—			4	7	2		+					
							•		2	0,	0	0	0



Next, students practice multiplying and dividing multi-digit numbers using algorithms that involve partial products and partial quotients. In both cases, students make connections across the different methods they see or use.

Section C: Multiplicative Comparison and World Travel

In this section, students use multiplication and division to make comparisons and solve real-world problems. They make estimates to simplify a problem, help with calculations, or assess whether a statement or a number is reasonable.

A school needs buses to take 375 people on a field trip.

- Bus Company A has small buses with 27 seats in each.
- Bus Company B has large buses with 48 seats in each.

Which bus company should the school choose?

Section D: Creation and Design

Throughout the course, students have participated in warm-up routines such as How Many Do You See, Exploration Estimation, Which One Doesn't Belong, True or False, and Number Talk.

In this section, they apply the mathematics they have learned to design warm-ups that use some of these routines. Add an item to complete the set.



Make sure there is at least one reason it belongs and one reason it doesn't belong.

Try it at home!

Near the end of the unit, ask your student to share the warm-up routines they created. Questions that may be helpful as they share:

- How did you design the routine?
- How does the routine relate to what you learned this year?
- What might you change to improve the routine?